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# CONTAMINATED SITES 2022

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*The activity has been implemented within the framework of national project  
**Information and providing advice on improving the quality of environment in Slovakia.**  
The project is cofinanced by Cohesion Fund of the EU under Operational programme Quality of Environment.*

# USING A NOVEL INDEX TO FIND THE MOST APPROPRIATE AGGREGATION FUNCTION FOR COMPOSITE HAZARD RATING OF A WASTE DISPOSAL SITE

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# Problems with waste dumps

- Leachate
- Fire & smoke
- Odour
- Groundwater contamination
- Slope failure

# Problem Statement

Hundreds of  
waste dumps for  
remediation

Kumar, A., Datta, M., Nema, A. K. Singh, R. K. and Gurjar, B. (2019). Response of Groundwater Contamination Hazard Rating Systems to Variations in Subsoil Conditions beneath Municipal Solid Waste (MSW) Dumps in Developing Countries. Arabian Journal of Geosciences. 12, Pg 405-. DOI: 10.1007/s12517-019-4560-4.

GW  
Contamination

Kumar, A., Datta, M., Nema, A. K. and Singh, R. K. (2017). Suitability of Hazard Rating Systems for Air Contamination from Municipal Solid Waste (MSW) Dumps and Improvements to Enhance Performance. Canadian Journal of Environmental Engineering and Science (Incorporated in Canadian Journal of Civil Engineering). 44. Pg 549 – 557. DOI: 10.1139/cjce-2016-0500.

Air  
Contamination

SW  
Contamination

Kumar, A., Datta, M., Nema, A. K. and Singh, R. K. (2016). An Improved Rating System for Assessing Surface Water Contamination Potential from MSW Landfills. Environmental Modeling and Assessment. 21. Pg 489-505. DOI: 10.1007/s10666-015-9493-z.

# Introduction

- A number of landfills in a region
  - Ranking for remediation
  - Ranking based on groundwater contamination hazard
- Landfills with multiple hazards associated with them
  - GW contamination, SW contamination, air contamination
  - How to rank these?

# Introduction

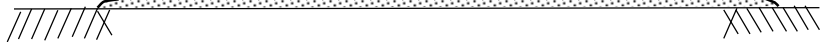
- Aggregation function
  - Aggregating various numbers e.g. air quality index

S. No.	Aggregation method	Function expression
1.	Maxima	$HR_{Comp} = \text{maximum}(HR_i)$
2.	Average or Simple Addition	$HR_{COMP} = \frac{1}{n} \sum_{i=1}^n HR_i$
3.	Weighted Sum	$HR_{COMP} = \sum_{i=1}^n w_i HR_i$

# Introduction

## Clustering index

Min. Rainfall;  
No GW users

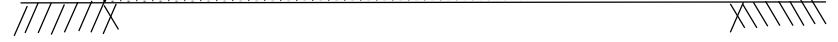


Clay soil

**Best Site**

**01**

Max. Rainfall;  
Densely populated area



Sandy soil

**Worst Site**

**1000**

# Introduction

## Clustering index

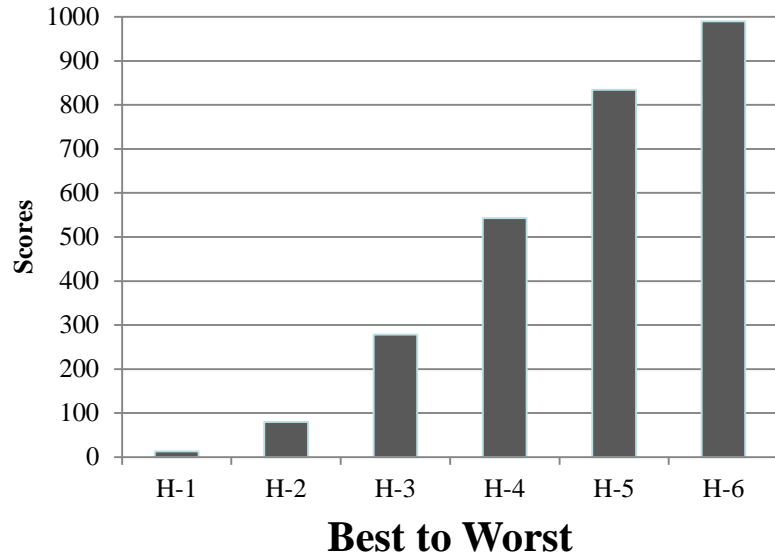
<b>1</b>	<b>200</b>	<b>400</b>	<b>600</b>	<b>800</b>	<b>1000</b>
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<b>1</b>	<b>100</b>	<b>200</b>	<b>300</b>	<b>400</b>	<b>1000</b>
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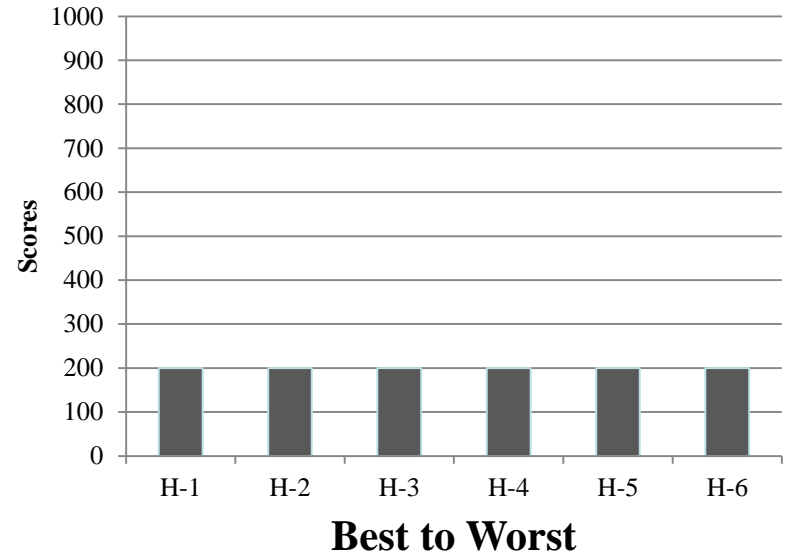


# Introduction

## Clustering index



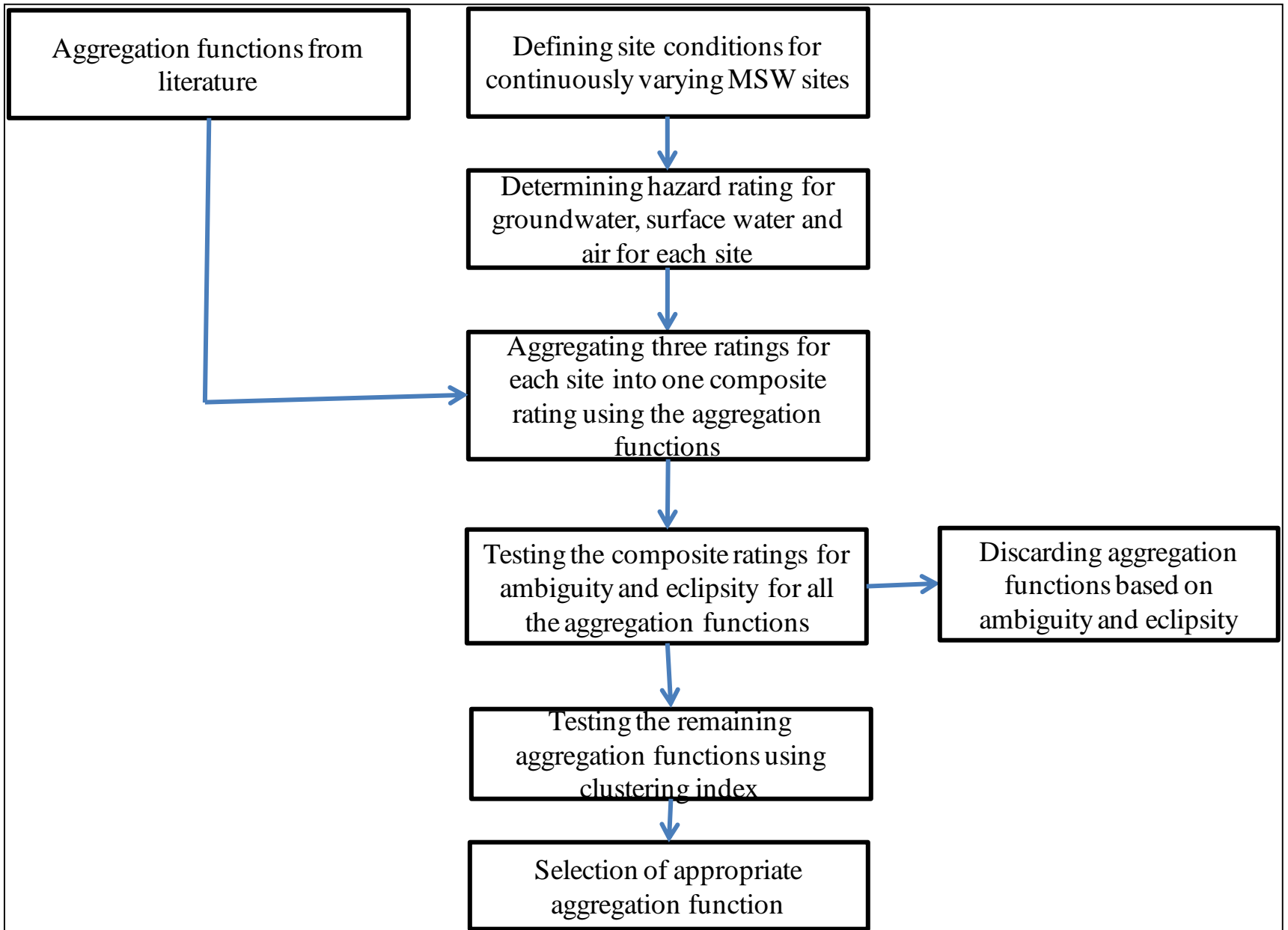
**Clustering Index = 0.0**



**Clustering Index = 1.0**

# Methodology

- Step 1: Application of individual new/modified rating systems to sites S-1 to S-27
- Step 2: Application of various aggregation functions from literature to determine composite hazard rating using individual scores from new rating systems
- Step 3: Screening of aggregation methods using ambiguity and eclipsity
- Step 4: Evaluation of initially selected aggregation functions using clustering
- Step 5: Selection of the aggregation method for composite hazard rating
- Step 6: Testing of the aggregation function with least clustering from step 5 for determining the priority for closure
- Step 7: Selection of aggregation function

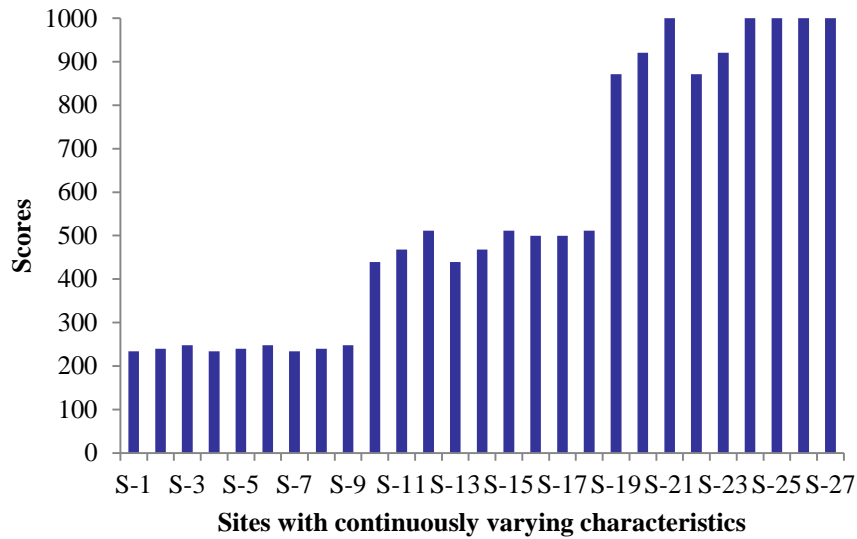


S. No.	Aggregation method	Function expression	Reference(s)
1.	Maxima	$HR_{Comp} = maximum(HR_i)$	[15]
2.	Average or Simple Addition	$HR_{COMP} = \frac{1}{n} \sum_{i=1}^n HR_i$	[22]
3.	Weighted Sum	$HR_{COMP} = \sum_{i=1}^n w_i HR_i$	[8]
4.	Unweighted multiplicative function	$HR_{Comp} = [\prod_{i=1}^n HR_i]^{\frac{1}{n}}$	[12]
5.	Weighted multiplicative or weighted geometric mean function	$HR_{Comp} = \prod_{i=1}^n HR_i^{w_i}$	[11]
6.	Root sum power function	$HR_{COMP} = [\sum_{i=1}^n HR_i^2]^{\frac{1}{2}}$	[19]
7.	Weighted root sum power function	$HR_{COMP} = [\sum_{i=1}^n w_i HR_i^r]^{\frac{1}{r}}$	[9]
8.	Root Mean Square	$HR_{COMP} = [\frac{1}{n} \sum_{i=1}^n HR_i^2]^{\frac{1}{2}}$	[9]
9.	Weighted root mean square function	$HR_{COMP} = \frac{[\frac{1}{n} \sum_{i=1}^n w_i HR_i^2]^{\frac{1}{2}}}{\sum_1^n w_i}$	[7]
10.	Unweighted ambiguity and eclipsity free function r=0.4	$HR_{COMP} = [\sum_{i=1}^n HR_i^{2.5}]^{\frac{1}{2.5}}$	[23]
11.	Weighted ambiguity and eclipsity free function r =0.4	$HR_{COMP} = [\sum_{i=1}^n w_i HR_i^{2.5}]^{\frac{1}{2.5}}$	[9]
12.	Subindex powered weight function	$HR_{COMP} = \sum_{i=1}^n HR_i^{w_i}$	[19]
13.	CEPI aggregation function	$HR_{Comp}$ $= maximum(HR_i) + (1000 - maximum(HR_i))$ $\times \frac{\prod_1^n HR_i}{\sum_1^n HR_i} \times \frac{1}{\sum_1^n HR_i}$	[24]

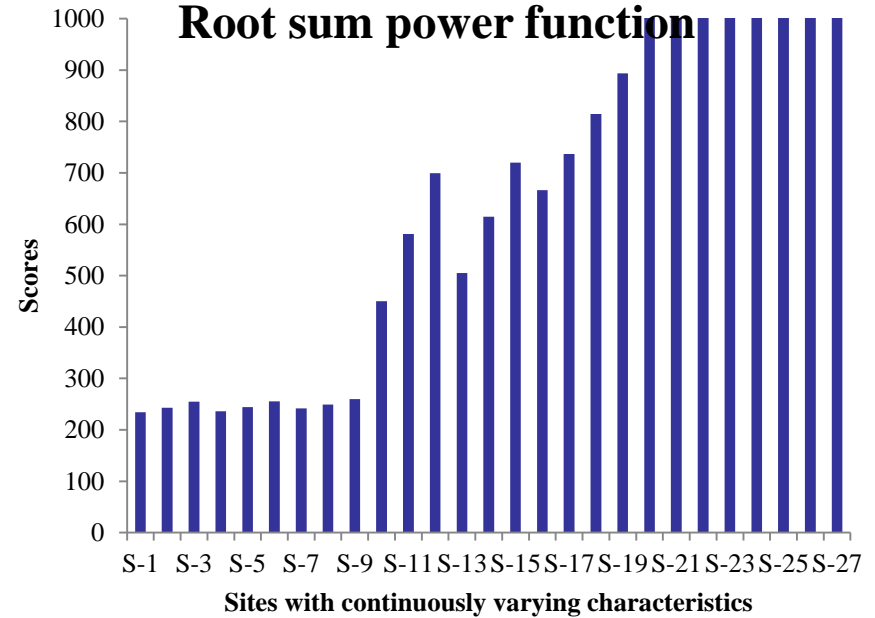


# Ambiguous functions

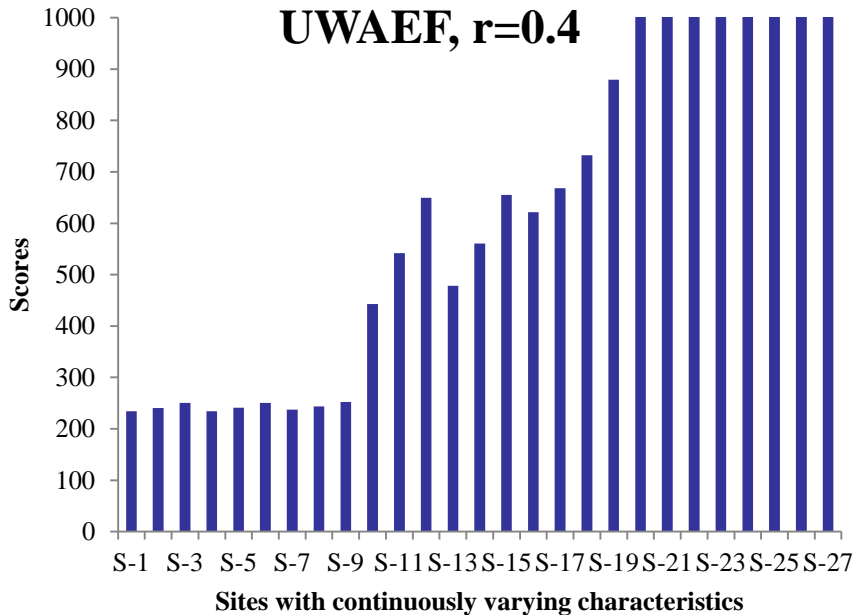
## Maxima



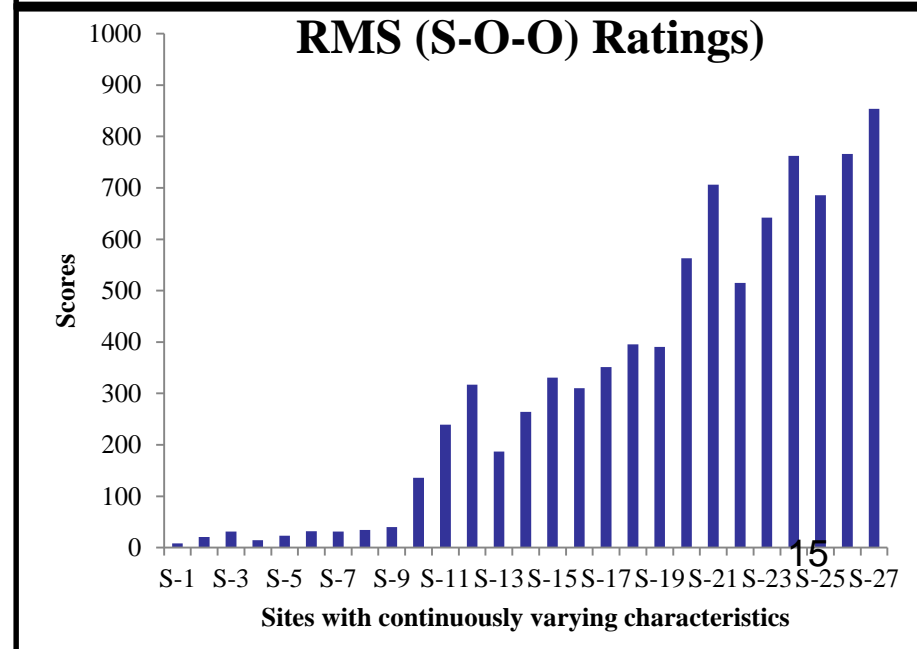
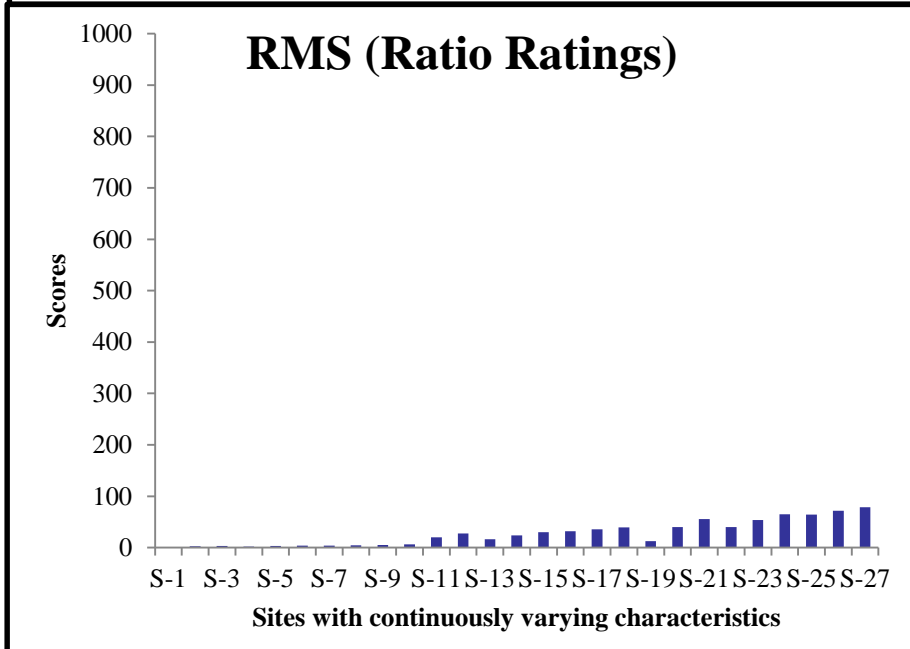
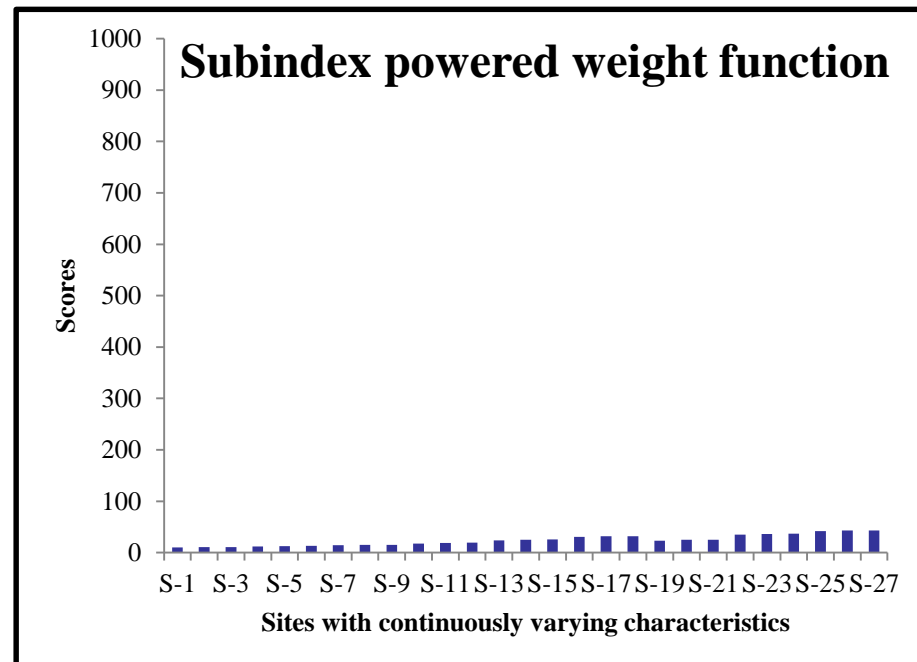
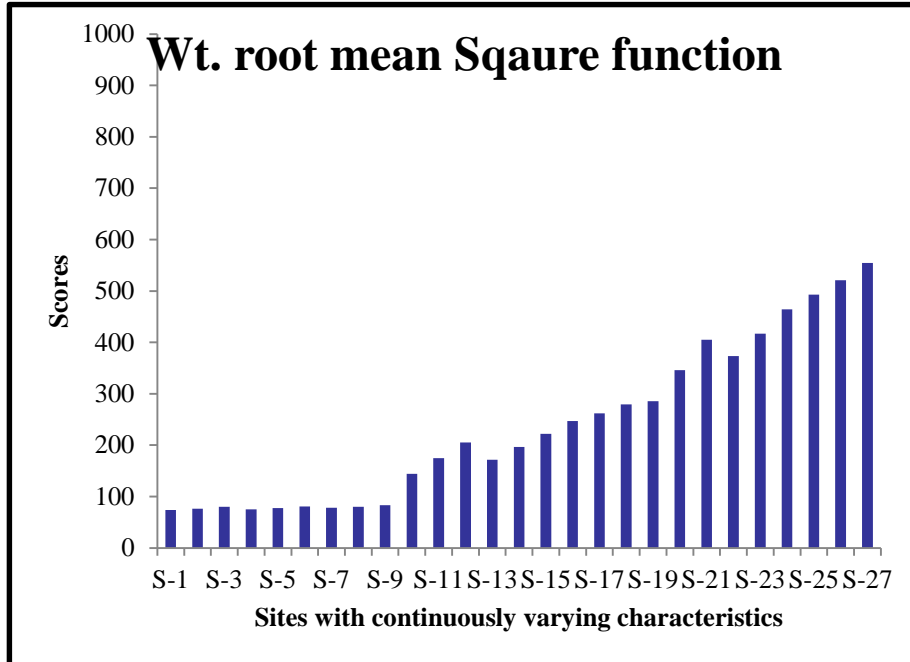
## Root sum power function



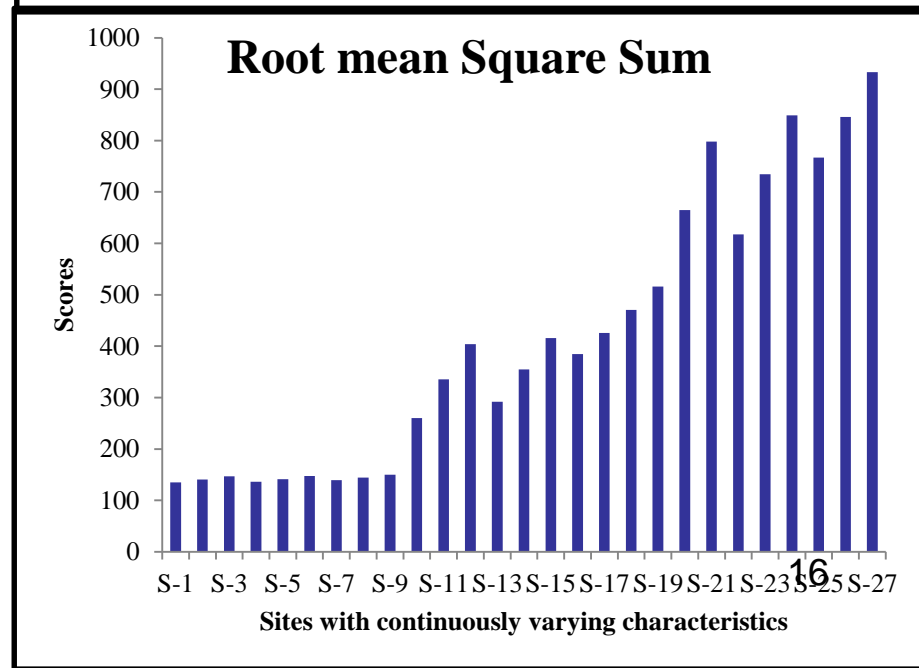
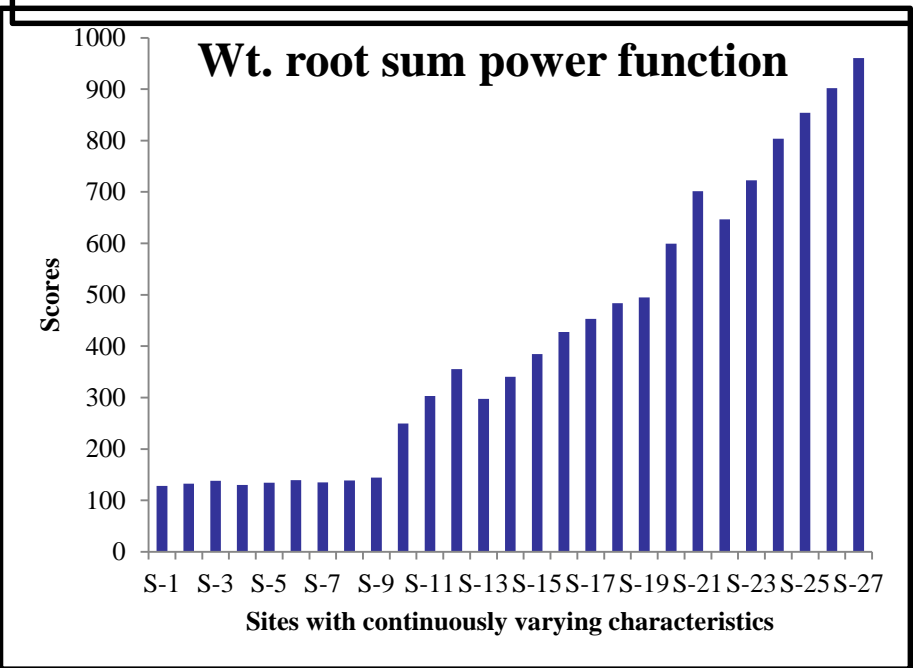
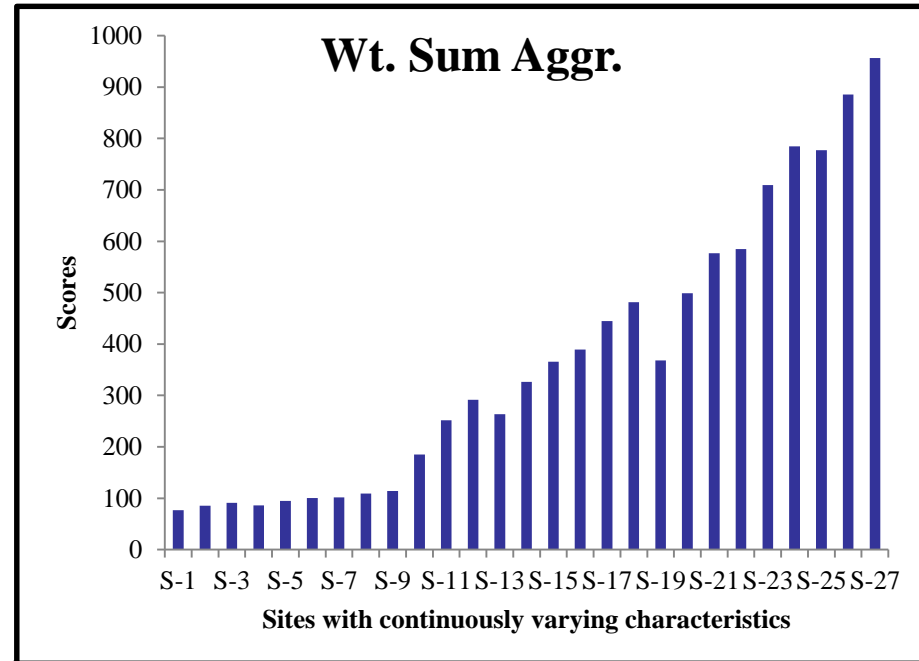
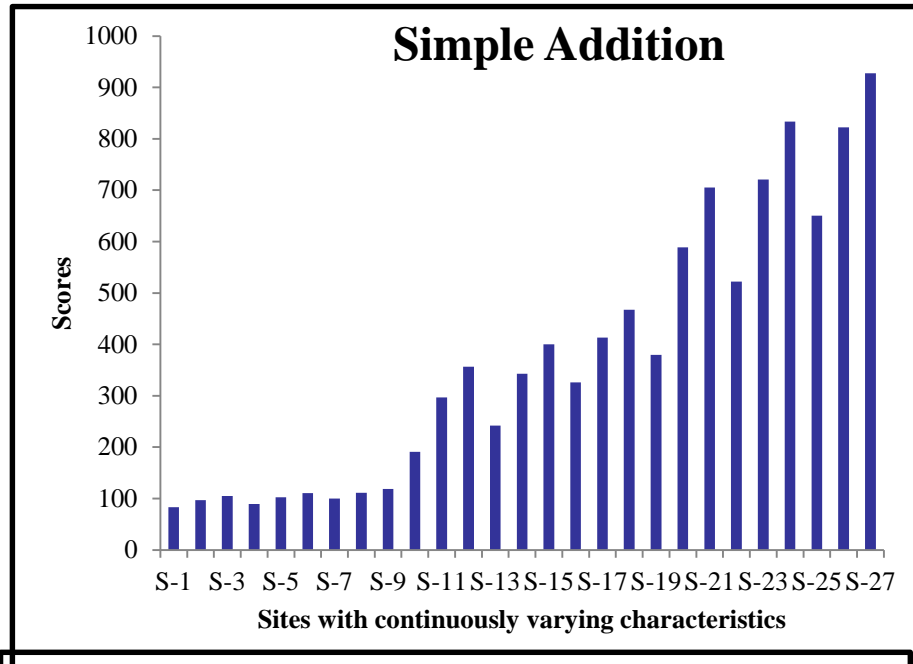
## UWAEF, $r=0.4$



# Eclipsed functions



# Non-ambiguous, non-eclipsed functions





# Clustering index

Aggregation function	Clustering index
Weighted sum aggregation	0.477
Weighted root sum power function	0.483
Root mean square sum	0.433
Wt. ambiguity & eclipsity free $r=0.4$	0.477
Simple addition	0.437
CEPI Aggregation	0.506

# Conclusions

- A large number of municipal waste disposal sites exist in India
  - Polluting the environment in a number of ways e.g. GW contamination, SW contamination and air contamination
  - Needs planning for remediation
  - Ranking may be one of the important means in planning
- The hazards posed by these dumps are of multiple types
  - Ranking should involve multiple hazards and be evolved as a composite ranking
  - For multiple hazards, an aggregation function is required.

# Conclusions

- The study tried to find the suitable function for aggregation
  - The aggregation functions may suffer from ambiguity or eclipsity
  - Moreover, the aggregated ranking may be clustered or confined in a narrow range, defying the purpose of ranking.
- The aggregation functions from literature were first tested for ambiguity and eclipsity.
  - The functions suffering from ambiguity or eclipsity were discarded.
  - The functions selected after the above step were tested for clustering.
  - Root mean square function was finally selected as an aggregation function.

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**Thank you**